

TABLE I  
TRIGONOMETRIC IDENTITIES

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$\exp(\pm j\theta) = \cos \theta \pm j \sin \theta$
$\cos \theta = \frac{1}{2} [\exp(j\theta) + \exp(-j\theta)]$
$\sin \theta = \frac{1}{j2} [\exp(j\theta) - \exp(-j\theta)]$
$\sin^2 \theta + \cos^2 \theta = 1$
$\cos^2 \theta - \sin^2 \theta = \cos(2\theta)$
$\cos^2 \theta = \frac{1}{2} [1 + \cos(2\theta)]$
$\sin^2 \theta = \frac{1}{2} [1 - \cos(2\theta)]$
$2 \sin \theta \cos \theta = \sin(2\theta)$
$\sin(\alpha \pm \beta) = \sin \alpha \cos \beta \pm \cos \alpha \sin \beta$
$\cos(\alpha \pm \beta) = \cos \alpha \cos \beta \mp \sin \alpha \sin \beta$
$\tan(\alpha \pm \beta) = \frac{\tan \alpha \pm \tan \beta}{1 \mp \tan \alpha \tan \beta}$
$\sin \alpha \sin \beta = \frac{1}{2} [\cos(\alpha - \beta) - \cos(\alpha + \beta)]$
$\cos \alpha \cos \beta = \frac{1}{2} [\cos(\alpha - \beta) + \cos(\alpha + \beta)]$
$\sin \alpha \cos \beta = \frac{1}{2} [\sin(\alpha - \beta) + \sin(\alpha + \beta)]$